

# Connections: position, velocity and acceleration

Known

$$\frac{d}{dt} [x(t)] = v(t)$$

$$\frac{d^2 x}{dt^2} = \frac{d}{dt} [v(t)] = a(t)$$

New

$$\int v(t) dt = x(t) + C$$

$$\int a(t) dt = v(t) + C$$

2 – dimensional distance from origin at position  $(x, y)$ :  $d = \sqrt{x^2 + y^2}$

1–dimensional distance from origin at position  $x$ :  $\sqrt{x^2} = |x|$

$\int_a^b v(t)dt$  is the displacement of the particle from  $t = a$  to  $t = b$ .

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Speed:  $|v| = s$

Speeding up if signs of  $a$  &  $v$  agree.

Slowing down if signs of  $a$  &  $v$  disagree.

$\int_a^b s(t)dt = \int_a^b |v(t)|dt$  is the total distance traveled by the particle.

In this context,  $s(t)$  is speed.  $s(t)$  is also often used for position in space.