Instructions: In the box below are the numbers $0-9$. Complete the following and cross off the number for each answer. If you complete all problems correctly, you will cross off each number exactly once!
$\begin{array}{llllll}0 & 1 & 2 & 3 & 4 & 5\end{array}$
$\begin{array}{lll}6 & 7\end{array}$
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a. Given that $\int_{1}^{6} x^{3} d x=\lim _{n \rightarrow \infty} \sum_{i=1}^{n}\left(1+\frac{b i}{n}\right)^{3} \frac{c}{n}$. Find $c-b$.

Use the table below to answer problems $b$ and $c$

| $x$ | 1 | 2 | 4 | 7 | 8 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $f(x)$ | 4 | -2 | 1 | 5 | -9 |

b. Use a left Riemann Sum with the four subintervals indicated by the data in the table to approximate $\int_{1}^{8} f(x) d x$
c. Use a right Riemann Sum with the four subintervals indicated by the data in the table to approximate $\int_{1}^{8} f(x) d x$

| $t$ | 0 | 1 | 3 | 7 | 8 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $v(t)$ | 0 | 2 | 0.5 | -1 | 2 |

d. The velocity of a particle, in meters per second, is given in the table above for selected times (in seconds). Use a left Riemann Sum with the four subintervals indicated in the table to approximate the total distance the particle travels, in meters, over the eight seconds.

$e$. The graph of the function $g$ is shown above for $0 \leq x \leq 4$. Of the following, which has the greatest value?

1. $\int_{0}^{4} g(x) d x$
2. Left Riemann Sum approximation of $\int_{0}^{4} g(x) d x$ with 4 subintervals of equal length
3. Right Riemann Sum approximation of $\int_{0}^{4} g(x) d x$ with 4 subintervals of equal length
4. Midpoint Riemann Sum approximation of $\int_{0}^{4} g(x) d x$ with 4 subintervals of equal length
5. Trapezoidal Sum approximation of $\int_{0}^{4} g(x) d x$ with 4 subintervals of equal length
$f$. It is known that $\lim _{n \rightarrow \infty} \sum_{k=1}^{n} \sqrt{\frac{2 k}{n}+1} \cdot \frac{1}{n}$ is equivalent to the expression $\int_{1}^{2} \sqrt{a x+b} d x$. Find $a+b$.

| $t$ | 0 | 1 | 2 | 3 | 4 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $h(t)$ | 0.25 | 1 | 1.25 | 2.75 | 3 |

g. Water is slowly poured into an empty glass. The height of the water, measured in inches, is recorded at selected times, in seconds, in the table above. Use a right Riemann Sum with four subintervals of equal length
indicated by the data in the table to approximate the value of $\frac{1}{4} \int_{0}^{4} h(t) d t$

h. The rate, in hundreds of people per hour, that the amount of people in an amusement park is changing is modeled by the function $R(t)$ above where $t=0$ corresponds to $12 P M$. If there are 300 people in the park at 12 PM , use a midpoint Riemann Sum with three equal subintervals to approximate the total number of people, in hundreds, in the park at 6PM.

| $x$ | 0 | 1 | 2 | 4 | 6 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $g(x)$ | 1 | 1.5 | 0.5 | 0.25 | 0.75 |

j. Use a trapezoidal approximation with 4 subintervals indicated by the data in the table above to approximate $\int_{0}^{6} g(x) d x$

k. The graph of $f(x)$ is above. use a midpoint Riemann Sum with three equal subintervals to approximate $\int_{0}^{6} f(x) d x$

